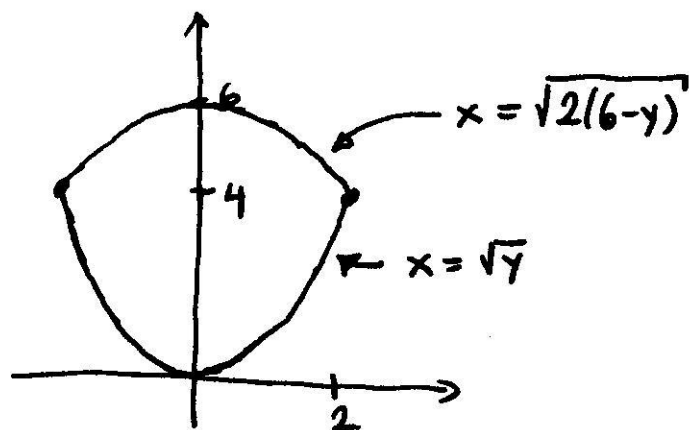


#26(b): I solve $y = 6 - \frac{1}{2}x^2$ and $y = x^2$ respectively
 (disks) for x , because I need the radius x as a function
 of y . These radii are ~~$x = \sqrt{2(6-y)}$~~ and
 $x = \sqrt{y}$ respectively



$$\begin{aligned} \text{Volume} &= \int_0^4 \pi (\sqrt{y})^2 dy + \\ &+ \int_4^6 \pi (\sqrt{2(6-y)})^2 dy = \\ &= \pi \int_0^4 y dy + \pi \int_4^6 (12-2y) dy = \underline{\underline{12\pi}} \end{aligned}$$

shells:

They are more convenient here, b/c

(a) we needn't solve for x , (b) we needn't split the
 integral:

$$\begin{aligned} \text{volume} &= \int_0^2 2\pi x \left(6 - \frac{1}{2}x^2 - x^2\right) dx = 2\pi \int_0^2 \left(6x - \frac{3}{2}x^3\right) dx \\ &= 2\pi \left[3x^2 - \frac{3}{8}x^4\right]_0^2 = 2\pi(12-6) = \underline{\underline{12\pi}} \end{aligned}$$

#26(c): We rotate about the y axis: $\text{Surface} = \int 2\pi x \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy$

• For y between 0 and 4: $x = \sqrt{y}$, $\frac{dx}{dy} = +\frac{1}{2\sqrt{y}}$

For y between 4 and 6: $x = \sqrt{12-2y}$, $\frac{dx}{dy} = \frac{-1}{\sqrt{12-2y}}$