

**Math 537 - Mathematical Principles of Continuum Mechanics - Fall 2024**

Tu/Th 16:05–17:20 in Ayres 112,

**Instructor:** Dr. Tim Schulze, 224C Ayres Hall, 974-4162, tschulze@utk.edu **Office Hours:** Tu/Th after class.

**Recommended Reading:**

- *A Mathematical Introduction to Fluid Mechanics* by A. J. Chorin & J. E. Marsden.
- *An Introduction to Fluid Dynamics* by G.K. Batchelor.
- *Fluid Mechanics: Volume 6 (Course of Theoretical Physics)* by L.D. Landau & E.M. Lifshitz.
- *Incompressible Flow* by R. L. Panton.
- *Elementary Fluid Dynamics* by D. J. Acheson.
- *Vorticity and Incompressible Flow* by A. J. Majda & A. L. Bertozzi.
- *Album of Fluid Motion* by M. Van Dyke.
- *Perturbation Methods in Fluid Mechanics* by M. Van Dyke.
- *Applied Analysis of the Navier-Stokes Equations* by Charles R. Doering & J. D. Gibbon.

**Course Prerequisites:** Vector calculus, experience solving partial differential equations.

**Course Description:** This course will provide a broad introduction to fluid mechanics and the mathematics associated with it. We will begin by discussing the equations for inviscid fluid flows (the Euler equations) and follow this by a discussion of the case of irrotational flows, where special mathematical techniques can be applied. We will then move on to viscous flows and the Navier-Stokes equations. Emphasis will be placed on exact solutions, asymptotic techniques and an analysis of energy dissipation.

Grading will be based on attendance/participation. There will be some suggested homework, but no exams in this course.

**Dates to note:**

- Sept. 5 - Householder Lecture 4th floor
- Oct. 8 - Fall break, no class
- Nov. 5 - Election Day, no class
- Nov. 28 - Thanksgiving break, no class
- Dec. 3 - Last day of class

## OUTLINE

1. Mathematical description of fluid flow
2. Flows that conserve energy
  - (a) The Euler Equations
  - (b) Elementary examples
    - i. Rotating flows
    - ii. Sources and sinks
  - (c) General results
    - i. Energy conservation
    - ii. Kelvin's Circulation Theorem
  - (d) Advanced solution techniques
    - i. Irrotational flow
    - ii. Conformal mapping
3. Flows that dissipate energy
  - (a) The Navier-Stokes Equations
  - (b) Elementary examples
    - i. Parallel flows
    - ii. Stagnation point flow
  - (c) General results
    - i. Energy dissipation
    - ii. Vorticity equation
  - (d) Advanced solution techniques
    - i. Similarity solutions
    - ii. Fourier-Laplace transforms
    - iii. Asymptotic methods